

Aufgabe 6

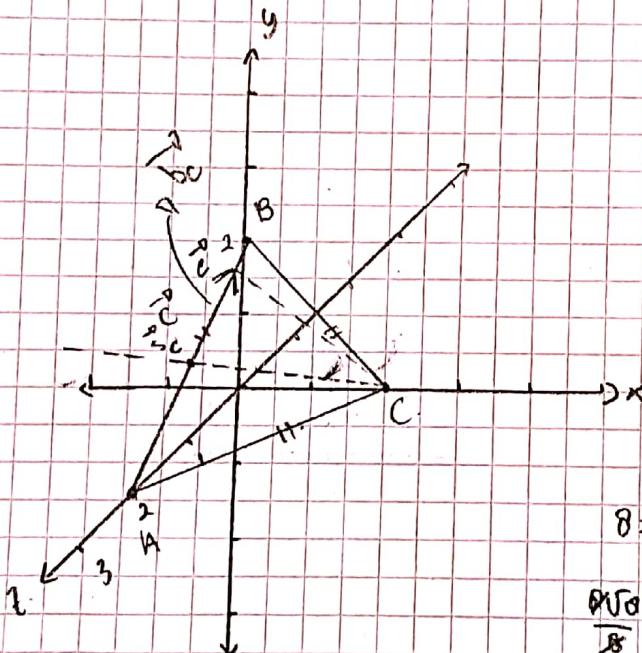
(i) $A(0;0;2), B(0;2;0), C(2;0;0)$

(1) $\vec{a} = \vec{AB} = \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 0 \\ 2 \\ -2 \end{pmatrix} = \sqrt{8} \rightarrow \|\vec{AB}\|$

$\vec{a} = \vec{BC} = \begin{pmatrix} 2 \\ 0 \\ 0 \end{pmatrix} - \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix} = \begin{pmatrix} 2 \\ -2 \\ 0 \end{pmatrix} = \sqrt{8} \rightarrow \|\vec{AB}\| \|\vec{BC}\|$

$\vec{b} = \vec{AC} = \begin{pmatrix} 2 \\ 0 \\ 0 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 2 \\ 0 \\ -2 \end{pmatrix} = \sqrt{8} = \|\vec{AC}\|$

ii).



$\vec{s}_c = \text{Seitenhalbierenden } AB$

$\hookrightarrow \frac{1}{2} \begin{pmatrix} 0 \\ 2 \\ -2 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix} = \text{oder } \vec{d}$

$\vec{cd} = \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix} - \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ -1 \\ -1 \end{pmatrix}$

$|\vec{cd}| = \sqrt{2^2 + 1^2 + 2^2} = \sqrt{6} \parallel \text{LE.}$

$8 = x \cdot \sqrt{8}$

$\frac{8\sqrt{8}}{8} = 2\sqrt{2}$

iii) $\vec{e} = (x, y, z) \in AB \rightarrow \vec{ce} = (x-2, y, z)$

$\vec{CH} \perp \vec{AB}$
 $\vec{CH} \cdot \vec{AB} = 0$

$(x-2) \cdot 0 + 2y \cdot 1 - 2z = 0$
 $2y = 2z$
 $y = z$

$x-2+2y-2z=0$
 $x=2$

iv) $A = \frac{1}{2} \|\vec{a}\| \|\vec{b}\| \sin 60^\circ$
 $= \frac{1}{2} \cdot \sqrt{8} \cdot \sqrt{8} \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{2}$
 $= 2\sqrt{3} \text{ FE}$

Orthogonalprojektion \vec{b}_c des Vektors \vec{b} auf den \vec{c}

$\vec{b}_c = \frac{\vec{b} \cdot \vec{c}}{\|\vec{c}\|^2} \cdot \vec{c}$
 $= \frac{0 \cdot 2 + 2 \cdot 0 + 0 \cdot 2 + (-2) \cdot (-2)}{(\sqrt{8})^2} \cdot \begin{pmatrix} 0 \\ 2 \\ -2 \end{pmatrix} = \frac{4}{8} \cdot \begin{pmatrix} 0 \\ 2 \\ -2 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 0 \\ 2 \\ -2 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$

$\vec{b}_c = \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$

$\|\vec{b}_c\| = \frac{\vec{b} \cdot \vec{c}}{\|\vec{c}\|} = \frac{4}{\sqrt{8}} = \sqrt{2}$